Modification of mesoporous silica magnetite nanoparticles by 3-aminopropyltriethoxysilane for the removal of Cr(VI) from aqueous solution

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Core-shell structure
Cr(VI) removal
Adsorption mechanism
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Abstract
Silica magnetite nanoparticles (S-MNPs) as core were embedded in mesoporous silica shells by using cetyltrimethylammonium bromide (CTAB) as a surfactant. Then, the resultant mesoporous silica-magnetite nanoparticles (M-S-MNPs) were modified with 3-aminopropyltriethoxysilane (APTES) as a coupling agent in dry hexane solvent. APTES-grafted mesoporous silica magnetite nanoparticles (A-M-S-MNPs) were characterized by XRD, FTIR spectroscopy, EDX, TEM, elemental analysis, TGA/DTA technique. Results demonstrate that the obtained A-M-S-MNPs were nearly spherical in shape with 25 nm thick mesoporous silica shell. The adsorption behavior of the nanocomposite was examined in removing of Cr(VI) ion with concentrations 20, 30 and 50 mg/L at optimum pH level of 2. In this study a pH swing adsorption was observed too. The adsorption kinetic data were modeled using pseudo-second-order kinetics and intraparticle diffusion equations. The obtained results for intraparticle diffusion model show that the adsorption mechanisms are different in low and in high concentrations of Cr(VI) ion. According to the parameters of the Langmuir isotherm, the maximum adsorption capacity \( q_m \) of A-M-S-MNPs for Cr(VI) increases as the temperature rises from 298 to 318 K. For better understanding of adsorption mechanism, quantum mechanical methods were applied. The results indicate that the electrostatic and hydrogen bond interactions between surface functional groups and \( \text{HCrO}_4^-/\text{Cr}_2\text{O}_7^{2-} \) ions have an important role in adsorption process. The easy separation from aqueous solution by an external magnetic field, rapid adsorption, regeneration, and reusability of A-M-S-MNPs are interesting points as an effective adsorbent for the removal of Cr(VI) ions.

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1. Introduction

In recent years, discharge of industrial wastewater containing heavy metal ions in nature has become one of the main environmental subjects due to the adverse effects of these ions on ecosystem and human health. Among the heavy metal ions, Cr(VI) with its wide application in different industries such as electroplating, leather tanning, and pigment industry has been extremely considered [1,2]. Depending on pH and redox conditions, chromium exists generally in two oxidation states Cr(VI) and Cr(III) in the aqueous solutions [3]. Cr(VI) has more mobility and solubility than another specie. Cr(III) is considered as a necessary element for controlling of glucose, lipid and protein metabolism in the human and animal body. While Cr(VI) is very dangerous to living organism due to its toxicity, mutagenic and carcinogenic properties [4,5]. Therefore, efficient removal of Cr(VI) from wastewaters is an important issue. Various treatment techniques have been used for the removal Cr(VI) from aqueous solutions such as ion exchange, precipitation, reverse osmosis and membrane processes. These methods have major drawbacks including incomplete metal removal, high reagents or energy requirements and generation of toxic sludge or secondary waste [6,7]. Therefore, the adsorption process as a high efficiency and low cost method can be used for the treatment of wastewater containing heavy metals [8,9].

Recently magnetite nanoparticles (MNPs) are applied as useful adsorbents for cleanup of environmental contaminants because of
their high surface area, easy separation from aqueous media under external magnetic fields [10,11]. Despite these positive features, MNPs are associated with several deficiencies such as aggregation, oxidation in air and instability under acidic conditions. For reduction of these undesirable features, bare MNPs are embedded into a host matrix [12]. Since mesoporous structures have large surface area, tunable pore size and well-defined pore structures [13,14], it is expected that suitable combination of MNPs and mesoporous structures as host matrix could make nanocomposites with novel properties. The mesoporous silica structure as a proper candidate for functionalization of silica surfaces [17]. Amino group in this molecule has a bi-functional nature and could adsorb anionic and cationic pollutants [18–20]. In general, two strategies post-synthesis or post-grafting and direct synthesis or co-condensation are applied for the modification of silica surfaces [21]. In post-synthesis method, modification performs by covalent bonding of organosilanes species with silanol cation of silica surface with organosilanes is usually carried out by refluxing in dry organic solvent [22].

In this work, A-M-S-MNPs were synthesized by embedding of S-MNPs in a mesoporous silica shell and then grafting of APTES molecules was performed by post-synthesis method in dry hexane. Size, morphology, nature of pores and amount of APTES loading for MNP in a mesoporous silica shell and then grafting of APTES were purchased from Sigma Aldrich. The de-ionized water was trimethylammonium bromide (CTAB), hydrochloric acid (HCl, 37%), ammonia solution (25%), were purchased from Merck. Cetylchloride (NaCl), ammonium nitrate (NH₄NO₃), 4-nitrobenzaldehyde, 1,5-diphenylcarbazide, ninhydrin, acetic acid chloride (NaOH), sodium hydroxide (NaOH), potassium nitrate (KNO₃), potassium dichromate (K₂Cr₂O₇), sodium chloride (NaCl), ammonium nitrate (NH₄NO₃, 4-nitrobenzaldehyde, 1,5-diphenylcarbazide, ninhydrin, acetic acid (CH₃CO₂H), sulfuric acid (H₂SO₄, 98%), (H₃PO₄, 85%), absolute ethanol, acetonitrile, tetraethyl orthosilicate (TEOS), sodium chloroacetate (CTAB), hydrochloric acid (HCl, 37%), were purchased from Sigma Aldrich. The de-ionized water was used in the synthesis and preparation of solutions.

2. Experimental

2.1. Materials

All reagents were of analytical grade and used as received. Iron (II) sulfate hexahydrate (FeSO₄·7H₂O), sodium hydroxide (NaOH), potassium nitrate (KNO₃), potassium dichromate (K₂Cr₂O₇), sodium chloride (NaCl), ammonium nitrate (NH₄NO₃), 4-nitrobenzaldehyde, 1,5-diphenylcarbazide, ninhydrin, acetic acid (CH₃CO₂H), sulfuric acid (H₂SO₄, 98%), (H₃PO₄, 85%), absolute ethanol, acetonitrile, tetraethyl orthosilicate (TEOS, >98%), 3-aminopropyltriethoxysilane (APTES, >98%), hexane (96%) and concentrated ammonia solution (25%), were purchased from Merck. Cetyltrimethylammonium bromide (CTAB), hydrochloric acid (HCl, 37%), were purchased from Sigma Aldrich. The de-ionized water was used in the synthesis and preparation of solutions.

2.2. Synthesis of adsorbent

The synthesis of MNPs were performed according to the reported procedure [23]. Briefly, two different solutions were prepared as follows: (1) dissolving of desired amount of NaOH and KNO₃ in 180 mL deionized water so that the final concentration of NaOH and KNO₃ reach to 7 × 10⁻² and 0.1 M respectively, (2) dissolving of desired amount of FeSO₄·7H₂O in 20 mL 10⁻² M H₂SO₄ to obtain a solution with concentration of 7.4 × 10⁻² M. After preparation the solutions, argon gas was bubbled into the solutions for 2 h. Then, solution (2) was added dropwise to basic solution under stirring. When the precipitation was completed, the container was placed in oil bath (90 °C) without stirring for 24 h. The obtained product was collected by a magnet and washed with deionized water.

To prepare of silica coated MNPs, 0.4 g of MNPs was added to a mixture containing 25 mL deionized water, 100 mL ethanol and 2 mL concentrated ammonia (25%) in a flask. The mixture was stirred vigorously for 30 min at 35 °C. Afterward, 0.3 mL of TEOS was added per hour until the total volume of TEOS reach to 2 mL. Finally, the resulting S-MNPs were collected by magnetic separation and washed with deionized water and ethanol several times.

To synthesize of M-S-MNPs, a desired amount of S-MNPs was dispersed in a mixture containing of deionized water, ethanol, concentrated ammonia and 1 g CTAB. After homogenization of the mixture by mechanical stirrer, 4 mL of TEOS was added dropwise to the mixture and the reaction was continued for 6 h at 30 °C. The product was washed with ethanol and water. For removing of surfactant and formation of mesoporous structure, two methods of calcination and solvent extraction are frequently used. In calcination, most of some surfactant groups are destroyed but at high temperature and then few numbers of APTES molecules can be grafted to the silica surface. Therefore, solvent extraction with ethanol and ammonium nitrate was selected as an appropriate method for removing of CTAB. 1.5 g of the sample was refluxed at 90 °C for 1 h in solution including 1 g ammonium nitrate in 80 mL ethanol. To complete extraction of CTAB, the procedure was repeated several times [24].

Since the silylating agent is polymerized in the presence of small amount of water, the APTES bottle was opened in a dry Ar-purged glove box and amino-functionalization experiment was performed under inert atmosphere by anhydrous hexane solvent. In addition, the silica surface adsorbs the humidity and for the desorption of physiosorbed water, the M-S-MNPs were heated at 180 °C for 3 h [25]. Then M-S-MNPs were placed in a 100 mL three-necked flask containing 30 mL of dry hexane. After Ar purge in solution for 1 h, 6 mmol APTES was added into the flask. Then the mixture reaction was heated under reflux at 68 °C for 24 h. In order to remove the unreacted APTES molecules, the resultant A-M-S-MNPs were washed by dry hexane three times.

2.3. Characterization methods

The XRD patterns of samples were obtained at room temperature using a X’Pert Pro MPD X-ray powder diffraction (Netherlands) with Cu Kα radiation (λ = 0.154 nm). The unite cell parameter (a₀) could be calculated from d₁₀₀ value by the following equation.

\[
a₀ = \frac{2d_{100}}{\sqrt{3} \lambda}
\]

(1)

Fourier transform infrared (FTIR) spectra of samples were recorded by Thermo Nicolet Avatar 370 FTIR spectrometer using the KBr disc technique. The spectra were collected in the 400–4000 cm⁻¹ range. The TEM image was taken on a Philips CM120 transmission electron microscope. The energy dispersive X-ray (EDX) was obtained on a LEO 1450VP scanning electron microscope (SEM) coupled with an Oxford 7335 EDX at acceleration voltage 20 and 5 kV. Thermogravimetric (TGA) and differential thermal (DTA) analysis were measured using a Shimadzu TGA/DTA 50 with heating rate of 20 °C/min under a nitrogen atmosphere. Carbon, nitrogen, hydrogen and oxygen contents were determined with a VARIAN elemental analyzer model CH 7 A (Germany).
concentration of Cr(VI) in aqueous solutions was determined by UV–vis spectrophotometer (Unico 2800) in the range 400–700 nm.

2.4. Adsorption experiments

Standard solutions of Cr(VI) in different concentrations are prepared from dissolving of K2Cr2O7 in deionized water. The HCl solution was used to adjust pH solutions to 2. In all adsorption experiments, 0.035 g of A-M-S-MNPs is placed in a double-walled glass jar containing 25 mL of Cr(VI) solution and stirred at different interval times. It should be noted that except the series of experiments related to the isotherm study, the others are performed at room temperature. To determine the residual concentration of Cr(VI) in the solution, the colorimetric was applied. Typically, 3 mL of the solution was used to adjust pH solutions to 2. In all adsorption experiments related to the isotherm study, the others are performed at different contact times. These peaks are matched with the standard Fe3O4 powder indexed to Miller indices 220, 311, 400, 422, 511, and 440, respectively. These peaks are also observed in other samples and are typical vibration bands of SiO2, including Si–O–Si stretching at 1090 and 1233 cm−1, and Si–O–H stretching vibration at 953 cm−1. Additionally, the broad peak in the range 3200–3750 cm−1 and the band at 1640 cm−1 are related to OH groups in silanol groups and adsorbed water molecules. These characteristic peaks are also observed in other samples. After grafting of APTES molecules, the intensity of (100) XRD peak decreases and higher order diffraction peaks (110 and 200) do not observe. This attributed to filling the pores of mesoporous structure by APTES molecules that decrease order of the mesoporous structure. In addition, the shift of (100) XRD peak to smaller angle in the SA-XRD pattern of A-M–S-MNPs is due to the expansion in unite cell after covalent linkage of aminosilane molecules on ordered mesoporous structure [27] (see Table 1a).

3. Results and discussion

3.1. Characterization of the adsorbent

3.1.1. XRD

The wide-angle XRD of A-M-S-MNPs is shown in Fig. 1. The strong diffraction peaks (2θ = 30.2, 35.5, 43.1, 53.5, 57, 62.6°) are indexed to Miller indices 220, 311, 400, 422, 511, and 440, respectively. These peaks are matched with the standard Fe3O4 powder diffraction data (JCPDS, card 19-0629). The position and relative intensity of all diffraction peaks are in accordance with the characteristic peaks of the face centered cubic magnetite structure. The crystal size (DxRD) by the Scherrer’s equation (DxRD = Kλ/βCosθ) at diffraction peak (2θ = 35.5°) was obtained 90 nm.

To confirm the mesoporous structure, the samples were examined by small angle X-ray diffraction (SA-XRD) as shown in Fig. 2. Table 1 shows the effect of grafting of APTES molecules on ordered mesoporous structure [27]. The M-S-MNPs show a typical mesoporous structure with three characteristic peaks corresponding to (100), (110) and (200) planes. After grafting of APTES molecules, the intensity of (100) XRD peak decreases and higher order diffraction peaks (110 and 200) do not observe. This attributed to filling the pores of mesoporous structure by APTES molecules that decrease order of the mesoporous structure. In addition, the shift of (100) XRD peak to smaller angle in the SA-XRD pattern of A-M–S-MNPs is due to the expansion in unite cell after covalent linkage of aminosilane molecules on ordered mesoporous structure [27].

3.1.2. FTIR spectra

The FTIR spectra of MNPs, S-MNPs, C-S-MNPs, M-S-MNPs and A-M-S-MNPs are displayed in Fig. 3. All of them have a peak around 580 cm−1 that accordance with Fe–O vibration band from magnetite phase. In the case of S-MNPs sample (Fig. 3; (b)), there are typical vibration bands of SiO2, including Si–O–Si bending at 468 cm−1, Si–O–Si symmetric stretching at 803 cm−1, Si–O–H stretching vibration at 953 cm−1, and Si–O–Si asymmetric stretching at 1090 and 1233 cm−1. Additionally, the broad peak in the range 3200–3750 cm−1 and the band at 1640 cm−1 are related to OH groups in silanol groups and adsorbed water molecules. These characteristic peaks are also observed in other samples (Fig. 3; (c–f)). For C-S-MNPs, three peaks at 1487, 2848 and 2917 cm−1 are attributed to bending, symmetric and asymmetric stretching vibration at 953 cm−1 and the band at 1640 cm−1 are related to OH groups in silanol groups and adsorbed water molecules. These characteristic peaks are also observed in other samples. After grafting of APTES molecules, the intensity of (100) XRD peak decreases and higher order diffraction peaks (110 and 200) do not observe. This attributed to filling the pores of mesoporous structure by APTES molecules that decrease order of the mesoporous structure. In addition, the shift of (100) XRD peak to smaller angle in the SA-XRD pattern of A-M–S-MNPs is due to the expansion in unite cell after covalent linkage of aminosilane molecules on ordered mesoporous structure [27] (see Table 1a).

Table 1. The 2θ,d-spacing of plane (100) and unit cell parameter a0 for M-S-MNPs and A-M-S-MNPs. The elemental analysis and APTES group content in mmol g−1 by three different methods.

<table>
<thead>
<tr>
<th>Sample</th>
<th>2θ (100)</th>
<th>2θ (110)</th>
<th>2θ (200)</th>
<th>d(100) (nm)</th>
<th>a0 (nm)</th>
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<td>M-S-MNPs</td>
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<td>4.42</td>
<td>4.81</td>
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<tr>
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<td>2.39</td>
<td>–</td>
<td>–</td>
<td>3.73</td>
<td>4.31</td>
</tr>
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</table>

<table>
<thead>
<tr>
<th>Sample</th>
<th>Elemental analysis (wt.%)</th>
<th>APTES loadinga (mmol/g)</th>
<th>APTES loadingb (mmol/g)</th>
<th>APTES loadingc (mmol/g)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A-M-S-MNPs</td>
<td>5.31</td>
<td>1.18</td>
<td>0.40</td>
<td>0.28</td>
</tr>
</tbody>
</table>

a Calculated from the elemental analysis data.
b Calculated from the TGA data, H and NH represent full and non-hydrolyzed forms of grafted APTES respectively.
c Measured by imine formation.
stretching vibration of $\text{CH}_2$ of CTAB template, respectively. After solvent extraction, no adsorption peaks were observed in the range of 2800–3000 cm$^{-1}$ for M-S-MNPs that indicate the effective removal of CTAB templates. Due to overlapping of the $\text{NH}_2$ bending and stretching vibrations with vibrations attributed to OH group in grafting APTES molecules on the surface of A-M-S-MNPs confirm by two peaks at 2863 and 2930 cm$^{-1}$. These peaks could be related to symmetric and asymmetric stretching modes of the $\text{CH}_2$ of aminopropyl groups, respectively [28]. After adsorption of Cr(VI) on A-M-S-MNPs, a new peak at 896 cm$^{-1}$ arises from Cr=O or Cr–O vibration of loaded Cr(VI) specie in Cr(VI)-A-M-S-MNPs [29].

### 3.1.3. TEM analysis

The morphology of the prepared A-M-S-MNPs was examined by TEM image. Fig. 4 shows that the A-M-S-MNPs are slightly irregular in shape and seem approximately spherical. Diameter of these nanoparticles are estimated about 150–200 nm. In addition, the mesoporous silica layer coated the core with some variation in shell thickness is about 25 nm. The polymerization of grafted aminopropyl groups on the surface of A-M-S-MNPs by silanization reaction leads to the attachment of their mesoporous silica layer together.

### 3.1.4. EDX spectrum

The EDX was used to analyze the elemental constituents of A-M-S-MNPs (Fig. 5). By applying acceleration voltage of 20 kV the K-level emission lines of Fe ($K_a = 6.41$ and $K_b = 7.06$ keV) are identified at high energies. The energy range below 2.5 keV where the $K_a$ emission lines of C, O and Si are observed at 0.28, 0.52, and 1.74 keV, respectively. The L-lines of Fe (0.70 keV) are also located in this energy range. These emission lines are confirmed the synthesis of Fe$_2$O$_4$ nanoparticles that are embedded in silica shells. Also the C peak is a direct evidence of attachment of APTES molecules to the nanocomposite surface that arises from propyl and ethoxy groups in APTES molecules. Also the N emission line (0.39 keV) that is related to the amine group ($\text{NH}_2$) in anchored APTES was not detected at high acceleration voltage of 20 kV. For observation of this peak, the acceleration voltage was reduced to 5 kV (inset picture of Fig. 5).

### 3.1.5. TGA/DTA analysis

The TGA/DTA curve of A-M-S-MNPs (Fig. 6) shows three weight loss peaks. The first peak (43°C) can be attributed to the desorption of water molecules from the surface of the silica layer. The decomposition of attached APTES molecules occurs at 342°C and the last weight loss peak at 466°C is accordance with the removal of surfactant [30]. The temperature for breakdown of grafted APTES groups is much higher than the boiling point of the pure APTES at 217°C. The results imply that the APTES molecules are bonded chemically (siloxane bond) to the surface of A-M-S-MNPs and exhibit a relatively high thermal stability [31]. The amount of weight loss (5.1 wt.%) at 342°C was used to determine the amount of APTES loading in A-M-S-MNPs. For this purpose, it was assumed that full and non-hydrolyzed forms of grafted APTES molecules were decomposed through siloxane bond (Si–O–Si) cleavage. The obtained results were listed in Table 1b.

### 3.1.6. Elemental analysis

Further investigation was carried out on the functionalized sample by elemental analysis. The obtained contents of nitrogen, carbon and hydrogen from this method are reported in Table 1b, which suggest a coverage of aminopropyl groups on the surface of
A-M-S-MNPs. Based on elemental analysis, the loading of APTES was calculated 0.28 mmol g$^{-1}$.

3.1.7. Imine formation

The total amount of amine groups was measured by a surface imine reaction. In this method, 4-nitrobenzaldehyde molecules (UV sensitive) react with amine groups under argon atmosphere and generate imine groups. This reaction can be returned toward producing precursors in the presence of a certain amount of water (Scheme 1). The regenerated 4-nitrobenzaldehyde concentration are determined spectrophotometrically at $\lambda = 282$ nm that is proportional to the numbers of reacted amine groups. The experimental procedure is consistent with the works that has been done already [32]. Typically, 0.01 g of A-M-S-MNPs was placed in a capped vial and was sonicated in an ultrasonic bath four times with 2 mL of acetic acid solution (0.08% v/v) in absolute ethanol. Next, 2 mL of 4-nitrobenzaldehyde solution (0.007 g in 10 mL of 0.08% acetic acid solution) was added to the suspension and allowed to react at 50 °C for 3 h. After removal of the supernatant, the nanoparticles were washed with absolute ethanol and sonicated for 2 min. In the hydrolysis step, the nanoparticles were immersed in 2 mL of acetic acid solution (0.2% v/v) in water and then mixture was stirred at 30 °C for 1 h. The hydrolyzed solution was separated from the nanoparticles with a magnet and the absorbance of regenerated 4-nitrobenzaldehyde measured at 282 nm. The concentration of this UV sensitive material in supernatant solution was calculated by the extinction coefficient ($\varepsilon_{\text{max}}$) that was $1.45 \times 10^{4}$ M$^{-1}$ cm$^{-1}$ in 0.2% acetic acid [33].

Based on the results in Table 1b, there is a good relation between obtained values of APTES loading from imine formation and TGA data for the non-hydrolyzed (NH) form. These values are comparable with the detected APTES by elemental analysis method and confirms that in our synthetic conditions the grafted APTES molecules are dominantly as non-hydrolyzed form.

3.1.8. Ninhydrin test

For more confirmation of the presence of amine groups on A-M-S-MNPs, the ninhydrin test was performed as reported previously [34]. At first, the un-reacted APTES molecules on the surface of A-M-S-MNPs were removed by washing with ethanol. Afterward,
0.032 g of the washed nanoparticles was mixed with 5 mL of 0.175 M ninhydrin solution in absolute ethanol. The mixture was sonicated for 40 min and was stirred at 90 °C. After cooling to room temperature, the mixture was centrifuged and the absorbance of the generated purple–blue complex in the supernatant was determined spectrophotometrically at 588 nm [35].

3.2. Pollutants removal

3.2.1. Effect of pH

Fig. 7 is shown the effect of solution pH on the amount of Cr(VI) removal. Maximum Cr(VI) adsorption occurs when the solution pH is 2. At this pH level, which is lower than pHpzc (is obtained by drift method), amino groups on the surface of adsorbent are protonated. For the Cr(VI) ion, five main species exist according to the following reactions. Based on these reactions, it can be calculated that under our condition (pH = 2) the dominate form of Cr(VI) is HCrO₄⁻ ion [36].

\[ H_2CrO_4 \rightleftharpoons HCrO_4^- + H^+ \quad K_1 = 1.58 \times 10^{-1} \]
\[ HCrO_4^- \rightleftharpoons CrO_4^{2-} + H^+ \quad K_2 = 3.16 \times 10^{-7} \]
\[ 2HCrO_4^- \rightleftharpoons Cr_2O_7^{2-} + H_2O \quad K_3 = 3.13 \times 10 \]
\[ HCrO_4^- \rightleftharpoons CrO_4^{2-} + H^+ \quad K_4 = 1.17 \]

Therefore, the better adsorption of A-M-S-MNPs at pH 2 can be attributed to an electrostatic interaction between HCrO₄⁻ and the protonated amino groups (–NH₃⁺) on the adsorbent surface (Reaction 1).

\[ Fe_3O_4@nSiO_2@mSi - O - Si(OEt)_2Pr - NH_3^+ + HCrO_4^- \rightleftharpoons Fe_3O_4@nSiO_2@mSi - O - Si(OEt)_2Pr - NH_3^+ \quad (1) \]

In the Reaction (1), Fe₃O₄@nSiO₂@mSi – O – Si(OEt)₂Pr – NH₃⁺ has shown the protonated A-M-S-MNPs, and HCrO₄⁻ as the dominate form of Cr(VI), respectively.

Since at pH values higher than 3, the –NH₂ groups could not be protonated completely and therefore the amount of Cr(VI) removal was decreased. As a result, Cr(VI) adsorption is related to its ionic forms in solution and the surface characteristics of the adsorbent that could be controlled by solution pH. Since low pH condition is observed for many industrial waste water, using of such pH as an optimum media for removal of Cr(VI) is realistic.

Furthermore, the DFT study of Cr(VI) adsorption in acidic condition shows that hydrogen bonds between HCrO₄⁻ and functional groups on the adsorbent surface (–NH₂ and surface Si–OH groups) play an important role in the adsorption process.

3.2.2. Effect of Cr(VI) concentration and contact time

In order to evaluate the adsorption efficiency of Cr(VI) on the surface of A-M-S-MNPs with time, three solutions were prepared at different concentrations (20, 30 and 50 mg/L). Fig. 8 shows that A-M-S-MNPs is a very effective adsorbent in removing of Cr(VI) within 30 min. The rapid decrease of Cr(VI) concentration within initial times attributed to high concentration of surface –NH₃⁺ groups and strong interaction between HCrO₄⁻ and adsorbent. The results also show that the reduction of concentration leads to lower adsorption of Cr(VI) on adsorbent surface at more than 30 min.

3.2.3. Adsorption kinetic

To study the adsorption kinetics of Cr(VI), pseudo first-order and pseudo second-order equations were used. The Eqs. (3) and (4) describe these kinetic models, respectively.

\[ \log(q_e - q_t) = \log q_e - \frac{k_1}{2.303}t \]  

(3)
\[
\frac{t}{q_t} = \frac{1}{k_2 q_e^2} + \left(\frac{1}{q_e}\right) t
\]

(4)

where \( q_e \) is the amount of adsorbed Cr(VI) at equilibrium (mg/g), \( q_t \) is the amount of Cr(VI) adsorbed on A-M-S-MNPS at time \( t \) (mg/g), \( k_1 \) (min\(^{-1}\)) is the pseudo-first-order rate constant and \( k_2 \) (g mg\(^{-1}\) min\(^{-1}\)) is the pseudo-second-order rate constant of adsorption.

The adsorption kinetics were studied for different solutions 20, 30 and 50 mg/L. Based on Fig. A.1 and correlation coefficients in Table 2, the kinetics for the removal of Cr(VI) fitted well with the pseudo-second order model. It means that in addition of \(-\text{NH}_3^+\) groups, the surface silanols can interact with HCrO\(_4^-\) ions too [37]. Another cause for the further confirmation of pseudo-second order kinetic model for adsorption Cr(VI) onto A-M-S-MNPs is related to the match of calculated \( q_e \) values, \( q_{e,\text{cal}} \), with experimental data. The \( k_2 \) values indicate that it decreases from 0.271 to 0.211 g/mg min as initial concentration increases from 20 to 50 mg/L (Table 2). This inverse relationship was observed by other researcher [6].

Adsorption is a three-step process consist of transport of adsorbate molecules solution to the external surface of the adsorbent (film diffusion or boundary layer diffusion), diffusion of the adsorbate into the pores of the adsorbent and adsorption of the adsorbate on the internal of adsorbent. Since adsorption step is very fast, the rate-controlling step in adsorption processes is the first two steps or combination of both steps. For the intraparticle diffusion rate equation is given by:

\[
q_t = k_i t^{0.5} + c
\]

(5)

where \( k_i \) is the intra-particle diffusion rate constant (mg/g min\(^{0.5}\)) and \( c \) is the intercept. The \( k_i \) value can be calculated from the slope of plot of \( q_t \) versus \( t^{0.5} \).

Time dependence of \( q_t \) for three different concentrations are represented in Fig. A.1c. In 20 mg/L solution, this dependency displays a two-part curve, which confirms two distinct kinetic regions; film diffusion and adsorption. But the story for 30 and 50 mg/L solutions are different such that increasing of concentration of Cr(VI) ion leads to three-part curves for these solutions. As is clear, a new section appears between film diffusion and adsorption steps that is related to intraparticle diffusion. It seems that this disparity comes from different adsorption mechanisms in low and high concentrations. In low concentrations, the film diffusion is the rate determining step of adsorption process while in high concentrations, the rate determining step changes. Since the second part of the curve in concentrations of 30 and 50 mg/L did not pass through the origin (\( c \neq 0 \)), it is concluded that not only intraparticle

**Table 2**

<table>
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<th>Concentration (mg/L)</th>
<th>Pseudo-second order</th>
<th>Intraparticle diffusion</th>
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<tr>
<td></td>
<td>( k_2 ) (g/mg min)</td>
<td>( q_{e,\text{cal}} ) (mg/g)</td>
</tr>
<tr>
<td>20</td>
<td>0.271 (+0.005)</td>
<td>13.947 (+0.154)</td>
</tr>
<tr>
<td>30</td>
<td>0.240 (+0.008)</td>
<td>19.724 (+0.226)</td>
</tr>
<tr>
<td>50</td>
<td>0.211 (+0.007)</td>
<td>30.211 (+0.360)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Concentration (mg/L)</th>
<th>( k_i ) (mg/g min(^{0.5}))</th>
<th>( c )</th>
<th>( \text{R}^2 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>30</td>
<td>2.102 (+0.030)</td>
<td>13.631 (+0.055)</td>
<td>0.985</td>
</tr>
<tr>
<td>50</td>
<td>2.820 (+0.071)</td>
<td>23.233 (+0.115)</td>
<td>0.980</td>
</tr>
</tbody>
</table>
3.2.4. Effect of ionic strength

The effect of ionic strength (KNO₃ and NaCl) on adsorption of Cr(VI) was studied at optimum pH. Fig. A.2 shows that the extent of Cr(VI) adsorption decreased with increasing of ionic strength from 10⁻³ to 10⁻¹ M. As it was discussed in pH effect, attractive electrostatic forces and hydrogen bonds between the adsorbent and HCrO₄⁻ ions are effective factors in adsorption. The ionic strength could decline the attractive forces by two ways: 1) neutralizing the negative charge of HCrO₄⁻ and 2) occupying positively adsorption sites (-NH₃⁺) [39]. In addition, charge reduction of adsorbate and adsorbent decreases electron sharing and weakens the formed hydrogen bonds. Therefore, the salts with decreasing attractive forces and hydrogen bond strength significantly reduces the adsorption of Cr(VI) on A-M-S-MNPs.

3.2.5. Adsorption isotherm model

To evaluate the adsorption process of Cr(VI) onto A-M-S-MNPs, the well-known Langmuir and Freundlich adsorption isotherm models were used to simulate experimental data. The linear form of the Langmuir isotherm can be represented by the following equation:

$$\frac{1}{q_e} = \frac{1}{q_m} + \frac{1}{bq_mC_e}$$

where qₑ is the amount of adsorbate on adsorbent at equilibrium (mg/g), Cₑ (mg/L) is the equilibrium concentration of adsorbate, qₑ (mg/g) is the maximum adsorption capacity and b (L/mg) is the Langmuir adsorption equilibrium constant. The values of b and qₑ were calculated from the slope and intercept of plot of 1/qₑ versus 1/Cₑ, respectively.

The Freundlich isotherm model can be depicted by the following equation:

$$\log q_e = \log K_f + \frac{1}{n} \log C_e$$

where K_f indicates the adsorption capacity and n is heterogeneity factor which for a favorable adsorption is larger than one (n > 1). The values of K_f and n can be obtained from the plotting of log qₑ versus log Cₑ.

The parameters of the Langmuir and Freundlich isotherm models are listed in Table 3. The high values of the correlation coefficients confirm that Langmuir isotherm fits the obtained data better than Freundlich model. It means that an uniform and monomolecular adsorption occurs on the A-M-S-MNPs. The results also show that the qₑ values increase from 33 to 50 mg/g with 20°C increasing in temperature. This indicates that the adsorption capacity of A-M-S-MNPs is extremely dependent to the temperature changes. The temperature dependency seems to come from conformational changes of functional groups on the nanoparticle surface. By heating, the rotational energy of functional groups increases and leads to destroy some of the hydrogen bonds between them. The –NH₃⁺ groups, as adsorption sites, become more available and their adsorption ability are increased. Furthermore, access to the adsorption sites inside pores becomes easier because of surface hydrogen bonds destruction (Scheme 2).

3.2.6. Thermodynamic parameters

The change in free energy ΔG°, enthalpy ΔH° and entropy ΔS° of adsorption can be obtained from the temperature dependence of adsorption isotherms. The following equations are used for the determination of the values of these thermodynamic parameters.

$$\Delta G^0 = -RT \ln K$$
$$\Delta G^0 = \Delta H^0 - T \Delta S$$

The values of ΔH° and ΔS° were obtained from the slope and intercept of a plot of lnK versus 1/T at different temperatures. The positive value of ΔH° confirms that the adsorption of Cr(VI) ions is an endothermic process. The negative values of ΔS° for the adsorption of Cr(VI) indicate that the adsorption is a spontaneous process (see Table 4). The positive value of ΔS° reflects the tendency of A-M-S-MNPs toward Cr(VI) ions in aqueous solutions and propose some structure changes in the adsorbent.

3.2.7. Regeneration and reusability

In order to evaluate the regeneration of A-M-S-MNPs, the desorption of Cr(VI) from adsorbate surface was performed by different NaOH solutions (0.01–0.1 M). The results show that the desorption efficiency can reach to 97% when the concentration of NaOH solution is 0.1 M. The mechanism of desorption under basic condition can be explained by the deprotonation of attached –NH₃⁺ groups on the adsorbent surface (Reaction 2). Due to the formation of –NH₂ groups on the surface, the electrostatic interaction between these groups and HCrO₄⁻ decreases and leads to the desorption process. Furthermore, this causes a decrease of the hydrogen bond power due to the less tendency of –NH₂ groups to form hydrogen bond. Since adsorption and regeneration process occur at low and high pH values, a pH swing adsorption is observed.

$$\text{Fe}_3\text{O}_4@\text{nSiO}_2@\text{mSi} - \text{O} - \text{Si(OrE)}_2\text{Pr} - \text{NH}_3^+ + \text{OH}^- \leftrightarrow \text{Fe}_3\text{O}_4@\text{nSiO}_2@\text{mSi} - \text{O} - \text{Si(OrE)}_2\text{Pr} - \text{NH}_2 + \text{H}_2\text{O}$$

As shown in Fig. 9, the adsorption capacity of Cr(VI) is about 30.2 mg/g in the first cycle and decreases to 24.5 mg/g in the fifth cycle. It assumes that this behavior comes from the mesoporous channels which are blocked with some HCrO₄⁻ ions in each cycle and decreases the adsorption capacity in the next cycles.

Comparison of our results with commercial adsorbents such as modified zeolites and activated carbon shows that A-M-S-MNPs have many advantages. A very high adsorption capacity is observed for our modified adsorbent with respect to the literatures [40–42]. A-M-S-MNPs could be separated easily from aqueous solutions due to having magnetic properties. In addition, the regeneration of this adsorbent take places at ambient temperature despite of activated
carbon [43]. All of these advantages make A-M-S-MNPs as a better adsorbent than commercial ones.

3.3. Theoretical adsorption energies

Furthermore, the adsorption of Cr(VI) on the different amino-functionalized silica surfaces was modeled by DFT calculations. For this purpose the adsorption of Cr(VI) on amino-functionalized silica surfaces were performed by using ONIOM methodology [44]. In our previous study, we designed 16 different conformations for amino-functionalized silica surfaces and they were classified in five categories [45]. In this study, the most stable configurations of each group were considered for investigation of adsorption of HCrO$_4$ on amino-functionalized silica surfaces. To simplify, the selected surfaces were named based on the name of their categories, for example, 3-ethoxy4 changed to 3-ethoxy. Given that the adsorption of HCrO$_4$ molecules onto amino-functionalized silica surfaces occurs in acidic environment, –NH$_2$ groups in two attached APTES molecules were protonated and changed to –NH$_3^+$.

For study of adsorption processes two optimized HCrO$_4$ molecules were placed on top of each designed surfaces and then the surface–HCrO$_4$ complexes were optimized. In addition, for increasing the accuracy of calculations of adsorption energies, the single point energy calculations were performed at high level of theory. Furthermore, the conductor-like Polarizable Continuum Model (CPCM, solvent = water) was used for solvation effects [46, 47].

The adsorption energies were calculated using the following equation:

$$
\text{Adsorption energy} = -\left[ E_{\text{surface} - \text{HCrO}_4} - \left( E_{\text{surface}} + 2E_{\text{HCrO}_4} \right) \right]
$$

where $E_{\text{surface} - \text{HCrO}_4}$ refers to the total energy of two HCrO$_4$ molecules on the surface while $E_{\text{surface}}$ and $E_{\text{HCrO}_4}$ are taken as the energies of surface without the HCrO$_4$ molecule and the HCrO$_4$ molecule, respectively.

Based on our calculation, the adsorption energy per HCrO$_4$ ion on the 4-ethoxy surface is 9.42 kJ mol$^{-1}$ while this value increases to 26.61, 44.60, 55.64, and 37.01 kJ mol$^{-1}$ from 3-ethoxy to 0-ethoxy surfaces, respectively. The obtained results indicate that the experimental adsorption energy ($\Delta H = 8.25$ kJ mol$^{-1}$) is similar to the theoretical value for the modeled 4-ethoxy surface. This result is accordance with outcomes from TGA, elemental analysis and imine reaction, which the grafted APTES molecules are dominantly as the non-hydrolyzed form.

Since the basis set super position error (BSSE) could affect the amount of calculated adsorption energies, its determination is important in accuracy of the obtained results [48]. Unfortunately, BSSE calculation with ONIOM method in solution media is not possible in Gaussian program. Therefore, an approximation method was used to estimate BSSE corrections. The BSSE corrections were computed for QM level in the gas phase for surface–HCrO$_4$ complexes to understand the accuracy of our applied basis set. Since the calculated BSSE corrections were calculated for QM level in gas phase, they could not add to the adsorption energy values and only are used for the estimation of the super position error of applied basis set. Analysis of the BSSE correction values for 4-ethoxy to 0-ethoxy surfaces locates in the range of 2.1–3.5 kJ mol$^{-1}$, respectively. This range indicates that our selected basis set is suitable and its super position error is negligible.

In addition, the nature of surface interactions was examined from these designed models. It was guessed that the electrostatic and hydrogen bond interactions play important role in the adsorption process. Charge distribution shows that the electrostatic attractions occurs between positive –NH$_3^+$ and negative HCrO$_4$ groups. This is while the bond length analysis determines the –N–H–O–Cr and –O–H–O–Cr hydrogen bonds interactions.
between adsorbent and adsorbates (Fig. 10). Formation of these hydrogen bonds between HCrO$_4^-$ ion and surface functional groups confirms our results about pseudo-second order kinetic model that in addition of $\text{NH}_3^+$ groups, the surface silanols can be as adsorption site.

4. Conclusions

In summary, A-M-S-MNPs as a novel magnetic sorbent with a mesoporous shell has been synthesized using APTES as the surface modification agent. XRD, FTIR spectrum, TEM, EDX, elemental analysis, TGA/DTA techniques were used for the chemical and structural characterization of the adsorbent. Furthermore, the imine reaction and ninhydrin test were applied to confirm that the grafted APTES molecules on the surface. Comparison between the amount of APTES loading from three methods TGA/DTA, elemental analysis and the imine reaction showed that the grafted APTES molecules exist predominantly as their non-hydrolyzed form. High adsorption capacity (34.25 mg/g at 298 K) for Cr(VI) removal at pH = 2 refers to a favorable degree of site-isolation of the functional groups (the distance between the two or more functional groups). In lower distance, intramolecular hydrogen bonds between adjacent amine groups form. This leads to blocking of the pores and decreasing of surface functional group protonation, which both of

Fig. 10. Adsorption of Cr(VI) ion on different amino-functionalized silica surfaces in acidic condition. Adsorption energies in kJ mol$^{-1}$ are given below each surface in parentheses. The oxygen, carbon, silicon, chromium and hydrogen atoms are shown as red, gray, green, purple and white colors, respectively. The electrostatic interactions are also clear from charge distribution of involved groups in 4-ethoxy–Cr complex. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
them decline the adsorption capacity. In higher distance than optimum one, the functional groups on the surface reduces and leads to lower adsorption capacity. As a result, A-M-S-MNPs could be used as a promising adsorbent for the removal of Cr(VI) from water and acidic industrial wastewater samples. In strong acidic condition they decline the adsorption capacity. As a result, A-M-S-MNPs could be optimum one, the functional groups on the surface reduces and leads to lower adsorption capacity. The theoretical adsorption energies could be the two effective interactions in the adsorption of Cr(VI) on the adsorbent. These results were obtained from charge distribution and bond length analysis. The theoretical adsorption energies confirm our suggestion about the non-hydrolyzed surface groups.

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Appendix A. Supplementary data

Supplementary data related to this article can be found at http://dx.doi.org/10.1016/j.micromeso.2015.07.008.

References